

LINEAR & HYPERBOLIC FUNCTIONS

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Lesson Description

In this lesson we:

- Sketch linear and hyperbolic functions
- Look at the effect of a and q on straight line graphs and hyperbolae



Summary

Linear Graphs

$y=mx+c$ / $y=ax+q$ (both are acceptable)

- For $a>0$, the higher the value of ' a ' (or m) the steeper the line.
- Changing the value of ' q ' (or c -the y intercept) will imply a vertical movement of the original graph

Hyperbolae

$$y = \frac{a}{x} + q$$

- For $a>0$ the graph lies in the first and third quadrants.
- For $a<0$ the graph lies in the second and fourth quadrants.
- $y = q$ is the horizontal asymptote
- $x = 0$ is the vertical asymptote
- The lines $y = x+q$ and $y = -x+q$ are the axes of symmetry of hyperbolae of the form
- $y = \frac{a}{x} + q$
- Changing values of ' a ' will either stretch or contract the original graph vertically.



Test Yourself

Question 1

State whether the following statement is true or false. If false provide a reason for your answer.

The given or chosen y value is called the independent variable.

Question 2

State whether the following statement is true or false. If false provide a reason for your answer.

The y asymptote of $f(x)=3x+4$ is $y=4$

Question 3

State whether the following statement is true or false. If false provide a reason for your answer.

The horizontal asymptote of $y = \frac{3}{x} + 2$ is $x=0$ and the vertical asymptote is $y=2$

Question 4

State whether the following statement is true or false. If false provide a reason for your answer.

The y intercept of $y = -\frac{4}{x} + 2$ is $y = 2$

Question 5

The value of the y intercept of $x + 2y = 5$ is:

- A 5
- B 2
- C 2.5
- D $\frac{2}{5}$

**Improve your Skills****Question 1**

Sketch the graph $f(x) = 2x+1$ with domain $[-2;2)$

Question 2

Draw the graph of $g(x) = 4/x$

Explain how the graph $h(x) = 4/x + 2$ compares to the original graph.

Draw $h(x)$ on the same set of axes as $g(x)$ showing all asymptotes and points of intersection.